Optimal Task Assignment and Path Planning using Conflict-Based Search with Precedence and Temporal Constraints

Extended Abstract

Yu Quan Chong
Carnegie Mellon University
Pittsburgh, PA, USA
yuquanc@andrew.cmu.edu

Jiaoyang Li
Carnegie Mellon University
Pittsburgh, PA, USA
jiaoyangli@cmu.edu

Katia Sycara
Carnegie Mellon University
Pittsburgh, PA, USA
sycara@andrew.cmu.edu

ABSTRACT

This paper examines the Task Assignment and Path Finding with Precedence and Temporal Constraints (TAPF-PTC) problem. We augment Conflict-Based Search (CBS) to generate task assignments and collision-free paths that adhere to precedence and temporal constraints for agents to maximize a user-defined objective.

KEYWORDS

Multi-Agent Task Assignment; Multi-Agent Path Finding; Precedence Constraints; Temporal Constraints

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1 INTRODUCTION

The Multi-Agent Path Finding (MAPF) problem [7] entails finding collision-free paths for a set of agents, guiding them from their start to goal locations. However, MAPF does not account for several practical task-related constraints. For example, agents may need to perform actions at goal locations with specific execution times, adhering to predetermined orders and timeframes. Moreover, goal assignments may not be predefined for agents, and the optimization objective may lack an explicit definition. To incorporate task assignment, path planning, and a user-defined objective into a coherent framework, this paper examines the Task Assignment and Path Finding with Precedence and Temporal Constraints (TAPF-PTC) problem. We augment Conflict-Based Search (CBS) [6] to simultaneously generate task assignments and collision-free paths that adhere to precedence and temporal constraints, maximizing an objective quantified by the return from a user-defined reward function in reinforcement learning (RL).

2 PROBLEM DEFINITION

TAPF-PTC is characterised by an undirected graph $G = (V, E)$, a set of $N$ agents $\{a_1, \ldots, a_N\}$, and a task $T$, which is a set of $M$ goals $\{g^1, \ldots, g^M\}$ with given temporal constraints. Each agent has a start vertex $s_i \in V$. Each goal $g^l$ is a tuple comprising a goal vertex $v^l$ and a goal action $a^l$.act and needs to be assigned to an agent $a_i$, requiring $a_i$ to reach $v^l$ and perform $a^l$.act for $\alpha(g^l)$ timesteps while waiting there. We use $[g^1_1, \ldots, g^1_N]$ to denote the sequence of $l$ goals assigned to agent $a_i$; so $\sum_{i=1}^N l_i = M$. We further use $\mu(g^l_1)$ and $\tau(g^l_1)$ to denote the timestep when agent $a_i$ starts and finishes performing action $a^l$.act at vertex $g^l_1$.v, respectively, so $\tau(g^l_1) - \mu(g^l_1) = \alpha(g^l_1)$. A path segment for an agent $a_i$ consists of the sequence of vertices and actions from the completion of $g^{l-1}_1$ to the completion of $g^l_j$, with the full path being the sequential concatenation of the path segments of $l_i$ goals. A solution to TAPF-PTC consists of a goal assignment and a set of conflict-free paths. Conflicts occur when certain constraints are violated: (1) We use vertex/edge constraints in [6] to avoid collisions, where no two agents can occupy the same vertex/edge at the same timestep. (2) We expand on the precedence constraints defined in [9], which consists of two goals and requires the execution or completion timestep of one to precede the other. (3) We introduce absolute temporal range constraints to fix the execution or completion timestep of goals within specified temporal ranges. (4) We introduce inter-goal temporal constraints to specify an upper bound between the difference in the execution or completion timesteps of two goals.

3 CBS-TA-PTC

We propose Conflict-Based Search with Task Assignment, Precedence, and Temporal Constraints (CBS-TA-PTC), an extension of CBS-TA [3] and CBS-PC [9], as shown in Algorithm 1. In cases where $M$ is significantly larger than $N$, we partition $T$ into subtasks $T_{sub}$, forming each $T_{sub}$ as a TAPF-PTC instance and solved by CBS-TA-PTC.

3.0.1 Goal Assignment. As our objective is defined by an RL return, determining the cost of assigning a goal to an agent requires knowledge of the agent’s entire path. So optimal assignment algorithms such as Hungarian [5] cannot be applied. Hence, we enumerate all possible combinations of agents and the goals in $T_{sub}$ and generate a root Constraint Tree (CT) node for each of them (line 1–7).

3.0.2 Conflict Resolution. Conflict resolution priority ordering: 1) Absolute temporal range, 2) Precedence, 3) Inter-goal temporal, and 4) Vertex/Edge. Absolute temporal range conflicts are the priority as they are based on temporal ranges independent from other goals. Precedence conflicts take priority over inter-goal temporal conflicts as actions should be performed in the correct order before being correctly spaced apart temporally. It is also likely that resolving
Algorithm 1 CBS-TA-PTC()

Input: Graph $G$, starts $(s_i)$, subtask $T_{sub}$, past solutions
Output: Path for each agent for given $T_{sub}$

1. for assignment in Combinations$(T_{sub})$ do
2. R $\leftarrow$ GenerateRootCTNode$(S, \text{past solutions, assignment})$
3. if R.return is maximum return then
4. return R.solution
5. end if
6. insert R to OPEN
7. end for
8. while OPEN not empty do
9. P $\leftarrow$ node from OPEN with the highest return
10. if P.return is maximum return then
11. return P.solution
12. end if
13. conflict $\leftarrow$ conflict in P w.r.t conflict resolution order
14. constraints $\leftarrow$ ResolveConflict(conflict)
15. for constraint in constraints do
16. Q $\leftarrow$ GenerateCTNode$(S, \text{past solutions, P, constraint})$
17. insert Q to OPEN
18. end for
19. end while

3.0.3 Low-Level Path Planning. Multi-Label $A^*$ (MLA*) [1] is used to generate a solution for a task assignment under the constraints on the CT node. A linear programming module using one of the HiGHS solvers [2, 4] is used to prune CT nodes that are unsolvable given their constraints from various conflicts before the MLA* search.

3.0.4 Theoretical Properties of CBS-TA-PTC. By decomposing the task into subtasks, CBS-TA-PTC is an incomplete and suboptimal algorithm. However, with the entire task as a subtask, CBS-TA-PTC can be shown to be optimal and complete by adapting Theorems 1 and 3 in [6] respectively, with the assumption that every trajectory is a Markov game with a fixed terminal timestep to ensure that the set of constraints that can be added to CT nodes is finite.

3.1 Results

3.1.1 Environment. Three agents have to defuse all bombs within a time limit. Each bomb has an ordered sequence of three colors with a sequence length of $[1, 3]$, a countdown timer that resets upon a correct defusing step, where the next sequence must be defused before the countdown, and a fuse timer that indicates the time when it must be fully defused. Certain bombs have dependencies, which dictates that the bomb it depends on must be fully defused or have exploded before any defusing steps on itself. Each agent has tools with 2 out of the 3 colors that remove the matching color from the bomb sequence. Failure to adhere to the above would result in the bomb exploding. A fully defused bomb gives a team reward proportionate to the sequence length of the bomb.

3.1.2 Baselines. We augment CBS-TA [3] to maximize return with vertex/edge constraints only, where, given the explosion of a bomb, CT nodes are generated in a naive manner with vertex conflicts for each agent for that timestep. It solves TAPF-PTC with its underlying precedence and temporal conflicts through a more inefficient best-first search through the CT relative to CBS-TA-PTC. For CBS-TA and CBS-TA-PTC, the return is generated by evaluating the solution from the low level, with past solutions from previous subtasks, on an oracle that simulates the environment based on the user-defined reward function and dynamics, which is typically implemented as a user-designed RL environment in practice [8]. Note that a maximum return solution is conflict-free by design.

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REFERENCES


