SFedRec: A Federated Learning Framework for Dynamic Session-based Recommendation

Extended Abstract

Hexiao Zhang[®] School of Computer and Information Science, Southwest University Chongqing, China zhanghexiao@email.swu.edu.cn

> Jiamou Liu[®] University of Auckland Auckland, New Zealand jiamou.liu@auckland.ac.nz

Yanni Tang[®] University of Auckland Auckland, New Zealand ytan370@aucklanduni.ac.nz

Wu Chen[®] * School of Computer and Information Science, Southwest University Chongqing, China chenwu@swu.edu.cn

ABSTRACT

Session-based recommendation systems are critical for capturing users' evolving interests in real-time interactions. However, applying such systems in a federated learning (FL) setting presents challenges related to decentralized data and privacy preservation. To address this, we propose SFedRec, a session-based federated recommendation framework that integrates long-term user preferences with dynamicd session-based behaviors. SFedRec builds decentralized heterogeneous knowledge graphs to model user-item interactions and social connections, utilizing a graph neural network to learn user representations while ensuring privacy through Local Differential Privacy (LDP). Extensive experiments on three real-world datasets demonstrate that SFedRec outperforms stateof-the-art federated recommendation models, showing significant improvements in both general and cold-start scenarios.

KEYWORDS

session-based recommendation; federated learning; heterogeneous knowledge graph; privacy preservation

ACM Reference Format:

Hexiao Zhang[®], Yanni Tang[®], Jiamou Liu[®], and Wu Chen[®]. 2025. SFedRec: A Federated Learning Framework for Dynamic Session-based Recommendation: Extended Abstract. In *Proc. of the 24th International Conference on Autonomous Agents and Multiagent Systems (AAMAS 2025), Detroit, Michigan, USA, May 19 – 23, 2025,* IFAAMAS, 4 pages.

1 INTRODUCTION

With the growing emphasis on data privacy, *federated learning (FL)* has emerged as a compelling solution to train machine learning models in decentralized environments without the need to collect

*Corresponding author

This work is licensed under a Creative Commons Attribution International 4.0 License. user data centrally [2, 7, 15–17, 23, 29, 47, 53, 60–62]. FL enables collaborative learning across clients while preserving user privacy, crucial with regulations like the General Data Protection Regulation (GDPR) [44]. While this approach has been successfully applied in various static tasks, its application in *recommender systems* – where user interactions are dynamic and personalized – presents a unique set of challenges.

In the context of FL, several works rely on centralized data for user preference modeling [1, 4, 18-20, 30, 31, 34, 40, 58]. They distribute the training of user-specific models across devices and share model updates, not raw data, with a central server. However, these models mainly learn static, long-term preferences and fail to capture dynamic user behavior well, especially in real-time scenarios like session-based recommendation systems [5, 8, 14, 21, 26, 32, 42, 45, 48, 50-52, 54]. More recently, graph neural networks (GNNs) are being integrated into federated recommendation systems to better capture the complex relationships [9, 24, 27, 28, 35, 36, 43, 49, 55, 59]. However, existing approaches using GNNs on static user-item bipartite graphs, which limits their ability to model session-based recommendations, where user preferences shift rapidly over short periods [11-13, 22, 37, 41, 46, 63]. Additionally, while social network can help with cold-start problem and accuracy [3, 25, 33, 38, 39, 57], most FL frameworks do not fully leverage the social context due to data privacy and integration complexity.

The primary goal of this research is to introduce a novel FL framework to address these gaps. Our aim is to capture the dynamic, session-based preferences of users in a privacy-preserving manner, while also leveraging social network information to improve recommendation performance in federated environments.

2 PROBLEM FORMULATION

Let U and I denote a sets of users and items, respectively. The dataset of user's historical behaviors \mathcal{D} contains all sessions of all users. Each user $u \in U$ is associated with a set of sessions denoted by $D_u \in (S_1^u, S_2^u, ..., S_{D_u}^u)$, where S_T^u is the T^{th} session of u. Each session S_T^u is a sequence of items clicked by an anonymous user, where $S_T^u[t] \in I$ denotes the I^{th} item in the session S_T^u . For brevity, we may drop the superscript u and/or superscript T in S_T^u , apart

Proc. of the 24th International Conference on Autonomous Agents and Multiagent Systems (AAMAS 2025), Y. Vorobeychik, S. Das, A. Nowé (eds.), May 19 – 23, 2025, Detroit, Michigan, USA. © 2025 International Foundation for Autonomous Agents and Multiagent Systems (www.ifaamas.org).

Model	Gowalla				Delicious				Foursquare			
	HR@10	MRR@10	HR@20	MRR@20	HR@10	MRR@10	HR@20	MRR@20	HR@10	MRR@10	HR@20	MRR@20
FedMF	18.27	7.63	22.48	8.34	12.58	6.39	15.46	8.42	22.35	7.55	25.24	8.06
FedPerGNN	31.36	15.58	36.98	16.41	26.14	12.97	29.92	14.19	40.93	18.56	49.20	20.18
FeSoG	34.25	17.02	40.12	18.66	32.33	15.20	40.67	16.68	47.66	23.91	56.45	25.06
SFedRec	37.53	17.35	42.05	19.48	32.92	15.95	42.42	17.10	49.69	24.50	57.02	25.64

Table 1: Experiment Results Compared with Baseline Methods in %

from the session component, we have a social network which is a graph S = (U, E) about social relations. The set of nodes in *S* is the user set *U*, and the set *E* of edges represents the social relationships between users. An edge (u, v) from *u* to *v* means that *u* is followed by *v*.

Given a sub-graph of local user-item interactions and social relationships, a user u_i stored in client c_i , the interaction data are denoted as D_u , We denote the $C = (c_1, c_2, ...)$ as clients set, each users' data is placed in different clients respectively, we define session-based federated social recommendation as the task of predicting the next project, that is, predicting the next item of a new session $S \notin D$, which needs to build a prediction model from all the users' data stored in their own private devices with a centralized server. Our work will be processed in a privacy preserving manner based on locally stored user historical data and auxiliary information extracted from local sub-graph which is built by the local user-user, user-item and item-item interaction.

3 METHODOLOGY

Our proposed method mainly comprises three components: longterm interests representation component, session-based representation component and federated learning component. To be specific, each component is explained as follows:

- Long-term interests representation component: This module firstly constructs local heterogeneous knowledge graph from all historical user behaviors \mathcal{D} and the social network *S* for each users to capture user-item interactions, item transitions, and social relationships, These sub-graphs endow the system with the ability to conduct local modeling of user behavior; then learns knowledge-enhanced long-term user and item representations by employing heterogeneous knowledge graph neural network to incorporate both historical trends and collaborative information from neighboring nodes in the graph.
- Session-based representation component: During the active session, this network focuses on modeling the transitions between items. By learning item embeddings at the session level, it can effectively incorporate real-time interaction information and capture the immediate interest changes of users in the current session. Meanwhile, it also takes full account of the long-term preferences of users, avoiding the situation of only focusing on session-level behaviors and ignoring the overall interest trends of users. The prediction part can comprehensively consider the long-term interests of users and the real-time needs of the current session, providing users with highly accurate next-item recommendations.

• Federated learning component: This module undertakes crucial tasks of data transmission and privacy protection in the federated learning framework. Its main responsibility is to upload the gradients of model parameters to the server. However, during the transmission of original gradient updates, there is a risk of sensitive information leakage. To effectively prevent this problem, this module adopts the Local Differential Privacy (LDP) technology. Specifically, before the client transmits parameters to the server, the LDP technology adds carefully controlled noise to the parameters. The addition of this noise can not only ensure the statistical usability of the data but also maximize the protection of user privacy information, making it difficult for attackers to obtain sensitive data from the transmitted parameters. Finally, the central server is responsible for collecting the parameters from various clients and aggregating these parameters. The aggregated results will be sent back to the clients for the clients to update their local models, thereby achieving the collaborative training and optimization of the entire federated learning system.

4 EXPERIMENT

We develop two experiments to validate our proposed SFedRec, we choose three representative benchmark public real-world datasets, i.e., *Gowalla [6]*, *Delicious [10]* and *Foursquare [56]*, to evaluate our proposed model. Table 1 shows the overall results of all baselines on three datasets, we highlight the best results in bold. Our SFedRec outperforms all the FedRec models by a big margin, this superiority of SFedRec can be mainly attributed to its innovative utilization of the multi-relation knowledge graph to learn the representation. The multi-relation knowledge graph enables SFedRec to capture a vast amount of complex information. It not only includes the direct relationships between users and items but also takes into account the indirect associations and semantic connections. By leveraging knowledge source, SFedRec can generate more accurate and comprehensive user and item representations, which demonstrates the effectiveness of our model.

5 CONCLUSION

In this paper, we first explore the challenge problem of dynamic recommendation and personalized in FedRec, considering the superiority of session-based recommendation systems in solving user dynamic interest problem. In the future, we will consider efficient aggregation of client private models and explore adversarial training and robustness enhancement techniques for dynamic federated recommendation.

REFERENCES

- Muhammad Ammad-Ud-Din, Elena Ivannikova, Suleiman A Khan, Were Oyomno, Qiang Fu, Kuan Eeik Tan, and Adrian Flanagan. 2019. Federated collaborative filtering for privacy-preserving personalized recommendation system. arXiv preprint arXiv:1901.09888 (2019).
- [2] Ravikumar Balakrishnan, Tian Li, Tianyi Zhou, Nageen Himayat, Virginia Smith, and Jeff Bilmes. 2022. Diverse client selection for federated learning via submodular maximization. In International Conference on Learning Representations.
- [3] Lesly Alejandra Gonzalez Camacho and Solange Nice Alves-Souza. 2018. Social network data to alleviate cold-start in recommender system: A systematic review. *Information Processing & Management* 54, 4 (2018), 529–544.
- [4] Di Chai, Leye Wang, Kai Chen, and Qiang Yang. 2020. Secure federated matrix factorization. IEEE Intelligent Systems 36, 5 (2020), 11–20.
- [5] Tianwen Chen and Raymond Chi-Wing Wong. 2021. An efficient and effective framework for session-based social recommendation. In Proceedings of the 14th ACM international conference on web search and data mining. 400–408.
- [6] Eunjoon Cho, Seth A Myers, and Jure Leskovec. 2011. Friendship and mobility: user movement in location-based social networks. In Proceedings of the 17th ACM SIGKDD international conference on Knowledge discovery and data mining. 1082–1090.
- [7] Xingbo Fu, Binchi Zhang, Yushun Dong, Chen Chen, and Jundong Li. 2022. Federated graph machine learning: A survey of concepts, techniques, and applications. ACM SIGKDD Explorations Newsletter 24, 2 (2022), 32–47.
- [8] Lei Guo, Hongzhi Yin, Qinyong Wang, Tong Chen, Alexander Zhou, and Nguyen Quoc Viet Hung. 2019. Streaming session-based recommendation. In Proceedings of the 25th ACM SIGKDD international conference on knowledge discovery & data mining. 1569–1577.
- [9] Chaoyang He, Keshav Balasubramanian, Emir Ceyani, Carl Yang, Han Xie, Lichao Sun, Lifang He, Liangwei Yang, Philip S Yu, Yu Rong, et al. 2021. Fedgraphnn: A federated learning system and benchmark for graph neural networks. arXiv preprint arXiv:2104.07145 (2021).
- [10] HetRec. 2011. Delicious. https://grouplens.org/datasets/hetrec-2011/
- [11] Chao Huang, Jiahui Chen, Lianghao Xia, Yong Xu, Peng Dai, Yanqing Chen, Liefeng Bo, Jiashu Zhao, and Jimmy Xiangji Huang. 2021. Graph-enhanced multi-task learning of multi-level transition dynamics for session-based recommendation. In Proceedings of the AAAI conference on artificial intelligence, Vol. 35. 4123-4130.
- [12] Dietmar Jannach, Bamshad Mobasher, and Shlomo Berkovsky. 2020. Research directions in session-based and sequential recommendation: A preface to the special issue. User Modeling and User-Adapted Interaction 30 (2020), 609–616.
- [13] Sara Latifi, Noemi Mauro, and Dietmar Jannach. 2021. Session-aware recommendation: A surprising quest for the state-of-the-art. *Information Sciences* 573 (2021), 291–315.
- [14] Jing Li, Pengjie Ren, Zhumin Chen, Zhaochun Ren, Tao Lian, and Jun Ma. 2017. Neural attentive session-based recommendation. In Proceedings of the 2017 ACM on Conference on Information and Knowledge Management. 1419–1428.
- [15] Tian Li, Anit Kumar Sahu, Ameet Talwalkar, and Virginia Smith. 2020. Federated learning: Challenges, methods, and future directions. *IEEE signal processing magazine* 37, 3 (2020), 50–60.
- [16] Tian Li, Anit Kumar Sahu, Manzil Zaheer, Maziar Sanjabi, Ameet Talwalkar, and Virginia Smith. 2020. Federated optimization in heterogeneous networks. *Proceedings of Machine learning and systems* 2 (2020), 429–450.
- [17] Xiaoxiao Li, Meirui Jiang, Xiaofei Zhang, Michael Kamp, and Qi Dou. 2021. Fedbn: Federated learning on non-iid features via local batch normalization. arXiv preprint arXiv:2102.07623 (2021).
- [18] Zhiwei Li, Guodong Long, and Tianyi Zhou. 2023. Federated recommendation with additive personalization. arXiv preprint arXiv:2301.09109 (2023).
- [19] Feng Liang, Weike Pan, and Zhong Ming. 2021. Fedrec++: Lossless federated recommendation with explicit feedback. In Proceedings of the AAAI conference on artificial intelligence, Vol. 35. 4224–4231.
- [20] Guanyu Lin, Feng Liang, Weike Pan, and Zhong Ming. 2020. Fedrec: Federated recommendation with explicit feedback. *IEEE Intelligent Systems* 36, 5 (2020), 21–30.
- [21] Chun Liu, Yuxiang Li, Hong Lin, and Chaojie Zhang. 2023. GNNRec: Gated graph neural network for session-based social recommendation model. *Journal* of Intelligent Information Systems 60, 1 (2023), 137–156.
- [22] Hanlin Liu, Zhuoming Xu, Qianqian Zhang, and Yan Tang. 2022. Integrating users' long-and short-term preferences for session-based recommendation. In 2022 IEEE 25th International Conference on Computer Supported Cooperative Work in Design (CSCWD). IEEE, 611–616.
- [23] Ji Liu, Jizhou Huang, Yang Zhou, Xuhong Li, Shilei Ji, Haoyi Xiong, and Dejing Dou. 2022. From distributed machine learning to federated learning: A survey. *Knowledge and Information Systems* 64, 4 (2022), 885–917.
- [24] Rui Liu, Pengwei Xing, Zichao Deng, Anran Li, Cuntai Guan, and Han Yu. 2024. Federated graph neural networks: Overview, techniques, and challenges. *IEEE Transactions on Neural Networks and Learning Systems* (2024).

- [25] Zhiwei Liu, Liangwei Yang, Ziwei Fan, Hao Peng, and Philip S Yu. 2022. Federated social recommendation with graph neural network. ACM Transactions on Intelligent Systems and Technology (TIST) 13, 4 (2022), 1–24.
- [26] Malte Ludewig and Dietmar Jannach. 2018. Evaluation of session-based recommendation algorithms. User Modeling and User-Adapted Interaction 28 (2018), 331–390.
- [27] Sichun Luo, Yuanzhang Xiao, and Linqi Song. 2022. Personalized federated recommendation via joint representation learning, user clustering, and model adaptation. In Proceedings of the 31st ACM international conference on information & knowledge management. 4289–4293.
- [28] Peihua Mai and Yan Pang. 2023. Vertical federated graph neural network for recommender system. In *International Conference on Machine Learning*. PMLR, 23516–23535.
- [29] Brendan McMahan, Eider Moore, Daniel Ramage, Seth Hampson, and Blaise Aguera y Arcas. 2017. Communication-efficient learning of deep networks from decentralized data. In *Artificial intelligence and statistics*. PMLR, 1273–1282.
- [30] Wu Meihan, Li Li, Chang Tao, Eric Rigall, Wang Xiaodong, and Xu Cheng-Zhong. 2022. Fedcdr: federated cross-domain recommendation for privacy-preserving rating prediction. In Proceedings of the 31st ACM International Conference on Information & Knowledge Management. 2179–2188.
- [31] Khalil Muhammad, Qinqin Wang, Diarmuid O'Reilly-Morgan, Elias Tragos, Barry Smyth, Neil Hurley, James Geraci, and Aonghus Lawlor. 2020. Fedfast: Going beyond average for faster training of federated recommender systems. In Proceedings of the 26th ACM SIGKDD international conference on knowledge discovery & data mining. 1234–1242.
- [32] Yitong Pang, Lingfei Wu, Qi Shen, Yiming Zhang, Zhihua Wei, Fangli Xu, Ethan Chang, Bo Long, and Jian Pei. 2022. Heterogeneous global graph neural networks for personalized session-based recommendation. In Proceedings of the fifteenth ACM international conference on web search and data mining. 775–783.
- [33] Vasileios Perifanis, George Drosatos, Giorgos Stamatelatos, and Pavlos S Efraimidis. 2023. FedPOIRec: Privacy-preserving federated poi recommendation with social influence. *Information Sciences* 623 (2023), 767–790.
- [34] Tao Qi, Fangzhao Wu, Chuhan Wu, Yongfeng Huang, and Xing Xie. 2020. Privacypreserving news recommendation model learning. arXiv preprint arXiv:2003.09592 (2020).
- [35] Yeqing Qiu, Chenyu Huang, Jianzong Wang, Zhangcheng Huang, and Jing Xiao. 2022. A privacy-preserving subgraph-level federated graph neural network via differential privacy. In International Conference on Knowledge Science, Engineering and Management. Springer, 165–177.
- [36] Liang Qu, Ningzhi Tang, Ruiqi Zheng, Quoc Viet Hung Nguyen, Zi Huang, Yuhui Shi, and Hongzhi Yin. 2023. Semi-decentralized federated ego graph learning for recommendation. In Proceedings of the ACM Web Conference 2023. 339–348.
- [37] Massimo Quadrana, Alexandros Karatzoglou, Balázs Hidasi, and Paolo Cremonesi. 2017. Personalizing session-based recommendations with hierarchical recurrent neural networks. In proceedings of the Eleventh ACM Conference on Recommender Systems. 130–137.
- [38] Shaghayegh Sahebi and William W Cohen. 2011. Community-based recommendations: a solution to the cold start problem. In Workshop on recommender systems and the social web, RSWEB, Vol. 60.
- [39] Suvash Sedhain, Scott Sanner, Darius Braziunas, Lexing Xie, and Jordan Christensen. 2014. Social collaborative filtering for cold-start recommendations. In Proceedings of the 8th ACM Conference on Recommender systems. 345–348.
- [40] Karan Singhal, Hakim Sidahmed, Zachary Garrett, Shanshan Wu, John Rush, and Sushant Prakash. 2021. Federated reconstruction: Partially local federated learning. Advances in Neural Information Processing Systems 34 (2021), 11220– 11232.
- [41] Wenzhuo Song, Shoujin Wang, Yan Wang, and Shengsheng Wang. 2021. Nextitem recommendations in short sessions. In Proceedings of the 15th ACM Conference on Recommender Systems. 282–291.
- [42] Yong Kiam Tan, Xinxing Xu, and Yong Liu. 2016. Improved recurrent neural networks for session-based recommendations. In Proceedings of the 1st workshop on deep learning for recommender systems. 17–22.
- [43] Changxin Tian, Yuexiang Xie, Xu Chen, Yaliang Li, and Xin Zhao. 2024. Privacy-Preserving Cross-Domain Recommendation with Federated Graph Learning. ACM Transactions on Information Systems 42, 5 (2024), 1–29.
- [44] Pravin Ullagaddi. 2024. GDPR: Reshaping the landscape of digital transformation and business strategy. International Journal of Business Marketing and Management 9, 2 (2024), 29–35.
- [45] Shoujin Wang, Longbing Cao, Yan Wang, Quan Z Sheng, Mehmet A Orgun, and Defu Lian. 2021. A survey on session-based recommender systems. ACM Computing Surveys (CSUR) 54, 7 (2021), 1–38.
- [46] Shoujin Wang, Qi Zhang, Liang Hu, Xiuzhen Zhang, Yan Wang, and Charu Aggarwal. 2022. Sequential/session-based recommendations: Challenges, approaches, applications and opportunities. In Proceedings of the 45th international ACM SIGIR conference on research and development in information retrieval. 3425–3428.
- [47] Zhen Wang, Weirui Kuang, Yuexiang Xie, Liuyi Yao, Yaliang Li, Bolin Ding, and Jingren Zhou. 2022. Federatedscope-gnn: Towards a unified, comprehensive and

efficient package for federated graph learning. In *Proceedings of the 28th ACM SIGKDD Conference on Knowledge Discovery and Data Mining.* 4110–4120.

- [48] Ziyang Wang, Wei Wei, Gao Cong, Xiao-Li Li, Xian-Ling Mao, and Minghui Qiu. 2020. Global context enhanced graph neural networks for session-based recommendation. In Proceedings of the 43rd international ACM SIGIR conference on research and development in information retrieval. 169–178.
- [49] Chuhan Wu, Fangzhao Wu, Lingjuan Lyu, Tao Qi, Yongfeng Huang, and Xing Xie. 2022. A federated graph neural network framework for privacy-preserving personalization. *Nature Communications* 13, 1 (2022), 3091.
- [50] Shu Wu, Yuyuan Tang, Yanqiao Zhu, Liang Wang, Xing Xie, and Tieniu Tan. 2019. Session-based recommendation with graph neural networks. In Proceedings of the AAAI conference on artificial intelligence, Vol. 33. 346–353.
- [51] Shu Wu, Yuyuan Tang, Yanqiao Zhu, Liang Wang, Xing Xie, and Tieniu Tan. 2019. Session-based recommendation with graph neural networks. In Proceedings of the AAAI conference on artificial intelligence, Vol. 33. 346–353.
- [52] Xin Xia, Junliang Yu, Qinyong Wang, Chaoqun Yang, Nguyen Quoc Viet Hung, and Hongzhi Yin. 2023. Efficient on-device session-based recommendation. ACM Transactions on Information Systems 41, 4 (2023), 1–24.
- [53] Han Xie, Jing Ma, Li Xiong, and Carl Yang. 2021. Federated graph classification over non-iid graphs. Advances in neural information processing systems 34 (2021), 18839–18852.
- [54] Chengfeng Xu, Pengpeng Zhao, Yanchi Liu, Victor S Sheng, Jiajie Xu, Fuzhen Zhuang, Junhua Fang, and Xiaofang Zhou. 2019. Graph contextualized selfattention network for session-based recommendation.. In *IJCAI*, Vol. 19. 3940– 3946.

- [55] Bo Yan, Yang Cao, Haoyu Wang, Wenchuan Yang, Junping Du, and Chuan Shi. 2024. Federated heterogeneous graph neural network for privacy-preserving recommendation. In Proceedings of the ACM on Web Conference 2024. 3919–3929.
- [56] Dingqi Yang. 2012. Foursquare. https://sites.google.com/site/yangdingqi/home/ foursquare-dataset
- [57] Liangwei Yang, Zhiwei Liu, Yingtong Dou, Jing Ma, and Philip S Yu. 2021. Consisrec: Enhancing gnn for social recommendation via consistent neighbor aggregation. In Proceedings of the 44th international ACM SIGIR conference on Research and development in information retrieval. 2141–2145.
- [58] Jingwei Yi, Fangzhao Wu, Chuhan Wu, Ruixuan Liu, Guangzhong Sun, and Xing Xie. 2021. Efficient-FedRec: Efficient federated learning framework for privacypreserving news recommendation. arXiv preprint arXiv:2109.05446 (2021).
- [59] Chunxu Zhang, Guodong Long, Tianyi Zhou, Peng Yan, Zijian Zhang, Chengqi Zhang, and Bo Yang. 2023. Dual personalization on federated recommendation. arXiv preprint arXiv:2301.08143 (2023).
- [60] Chen Zhang, Yu Xie, Hang Bai, Bin Yu, Weihong Li, and Yuan Gao. 2021. A survey on federated learning. *Knowledge-Based Systems* 216 (2021), 106775.
- [61] Huanding Zhang, Tao Shen, Fei Wu, Mingyang Yin, Hongxia Yang, and Chao Wu. 2021. Federated graph learning–a position paper. arXiv preprint arXiv:2105.11099 (2021).
- [62] Ke Zhang, Carl Yang, Xiaoxiao Li, Lichao Sun, and Siu Ming Yiu. 2021. Subgraph federated learning with missing neighbor generation. Advances in Neural Information Processing Systems 34 (2021), 6671–6682.
- [63] Xiangde Zhang, Yuan Zhou, Jianping Wang, and Xiaojun Lu. 2021. Personal interest attention graph neural networks for session-based recommendation. *Entropy* 23, 11 (2021), 1500.